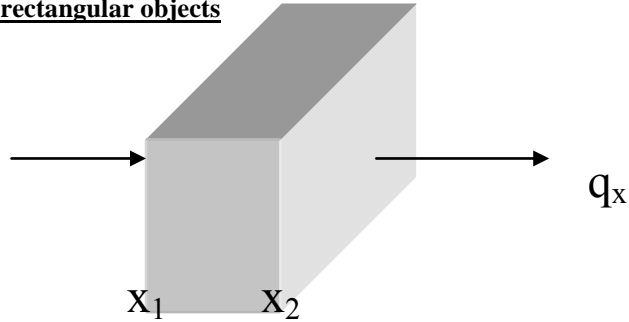


STEADY -STATE HEAT CONDUCTION

Steady state means that temperature in an object may vary by location

Conduction in rectangular objects

Fourier's law describes the rate of heat conduction in a solid.

Boundary Conditions

$$x = x_1 \quad T = T_1$$

$$x = x_2 \quad T = T_2$$

Separating the variables,

Integrating from x_1 to x (some interior location within the slab)

$$\int_{x_1}^x \frac{q_x}{A} dx = - \int_{T_1}^T k dT$$

$$T = T_1 - \frac{q_x}{kA} (x - x_1)$$

$$q_x = -kA \frac{(T - T_1)}{(x - x_1)}$$

if integrated from x_1 to x_2

where L = thickness of the slab.

Thermal Resistance concept:

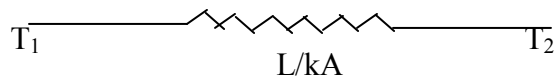
In the flow of electricity, the electrical resistance is determined from the ratio of electric potential divided by the electric current. Similarly, we may consider heat resistance as a ratio of the driving potential (temperature difference) divided by the rate of heat transfer.

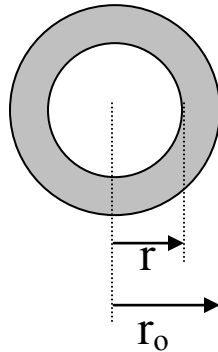
Thus,

$$R_{\text{conduction}} = \frac{T_1 - T_2}{q_x}$$

or,

units of resistance = °C/W



Conduction in Cylindrical objects**HEAT TRANSFER IN A TUBULAR PIPE**

Fourier's Law in cylindrical coordinates

$$q_r = -kA \frac{dT}{dr}$$

Boundary Conditions

$$\begin{aligned} T &= T_i \quad \text{at} \quad r = r_i \\ T &= T_o \quad \text{at} \quad r = r_o \end{aligned}$$

Separating the variables

Integrating

$$\frac{q}{2\pi L} \ln r \Big|_{r_i}^{r_o} = -k \Big| T \Big|_{T_i}^{T_o}$$

$$\frac{q}{2\pi L} (\ln r_o - \ln r_i) = -k (T_o - T_i)$$

$$q = \frac{2\pi L k (T_i - T_o)}{\ln \left(\frac{r_o}{r_i} \right)}$$

Using the preceding equation, we may write the conductive resistance in cylindrical coordinates as: